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The Bayesian Approach to Inverse Problems: Overview

Invited Talks at the University of Cambridge, UK

Preamble

- ▶ This is **no** commercial for the Bayesian approach to inverse problems.
- ▶ The term “*Bayesian*” is en vogue and used all too frequently.
- ▶ Especially it is often used to reformulate well established methods.
- ▶ This provokes (justified) resistance and reservation.
- ▶ Motivation of this talk: Counteract some common objections and highlight some interesting features of the Bayesian approach.



Overview

Three talks on the Bayesian approach to inverse problems.

Talk 1: "*Theoretical Aspects*".

Talk 2: "*Computational Aspects*".

Talk 3: "*Hierarchical Bayesian Approaches to EEG/MEG Source Reconstruction*".

Overview

Three talks on the Bayesian approach to inverse problems.

Talk 1: “*Theoretical Aspects*”.

- ▶ Deterministic, statistical and Bayesian perspective on inverse problems.
- ▶ Basic principles and concepts of Bayesian inference and modeling applied to inverse problems;
- ▶ Connections to variational regularization and ridge regression;
- ▶ Point estimates: Common myths and recent results;
- ▶ Advanced topics and some recent trends;
- ▶ What might be *real* benefits of Bayesian inference over other approaches?

Talk 2: “*Computational Aspects*”.

Talk 3: “*Hierarchical Bayesian Approaches to EEG/MEG Source Reconstruction*”.

Overview

Three talks on the Bayesian approach to inverse problems.

Talk 1: “*Theoretical Aspects*”.

Talk 2: “*Computational Aspects*”.

- ▶ Exemplary application: High-dimensional inverse problems using sparsity constraints;
- ▶ Basic principles and algorithms of Markov chain Monte Carlo (MCMC) based posterior inference;
- ▶ Iterative optimization and sampling;
- ▶ More advanced topics and some recent trends;

Talk 3: “*Hierarchical Bayesian Approaches to EEG/MEG Source Reconstruction*”.

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- ▶ Indispensable tools for neuroimaging;
- ▶ Challenging, severely ill-posed inverse problem;
- ▶ Various demands from the application;
- ▶ Hierarchical Bayesian modeling (HBM) to address various uncertainties;
- ▶ Own results on fully-Bayesian inference for HBM;



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